



Boyles' Law
P and V

Avogadro's Law
Equal volumes of gases
at the same P & T have
equal # particles



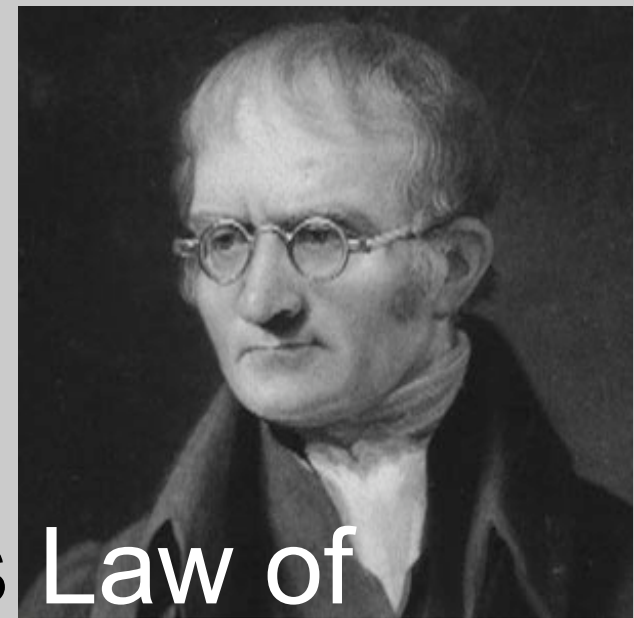
Gas Laws



Charles' Law
V and T



Gay-Lussac's Law
P and T



Dalton's Law of
Partial Pressure
 $P_1 + P_2 + P_3 \dots = P_{\text{total}}$

The Combined Gas Law

$$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2}$$

Remember This ??

The Combined Gas Law

The “Before and After” Gas Law

- Consider 0.5 L of gas in sealed syringe in a 50°C water bath with a pressure of 200 mmHg. The syringe is compressed to 0.1 L held at 50°C, what will be the new pressure?

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The Combined Gas Law

The “Before and After” Gas Law

- Consider 0.5 L of gas in **sealed** syringe in a **50°C** water bath with a pressure of 200 mmHg. The syringe is compressed to 0.1 L held at **50°C**, what will be the new pressure?

$$\frac{P_1 V_1}{\cancel{n_1} \cancel{T_1}} = \frac{\cancel{P_2} V_2}{\cancel{n_2} \cancel{T_2}}$$

$$P_2 = 1000 \text{ mmHg}$$

The Combined Gas Law

The “Before and After” Gas Law

- 2 L of oxygen gas in a sealed, rigid metal cylinder is at 0.80 atm at 25°C. To what temperature, in Celsius should the gas be changed to reduce the pressure to 0.30 atm?

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The Combined Gas Law

The "Before and After" Gas Law

- 2 L of oxygen gas in a **sealed**, **rigid** metal cylinder is at 0.80 atm at 25°C. To what temperature, in Celsius should the gas be changed to reduce the pressure to 0.30 atm?

$25^{\circ}\text{C} + 273 = 298\text{ K}$

$$\frac{P_1 \cancel{V_1}}{\cancel{n_1} T_1} = \frac{P_2 \cancel{V_2}}{\cancel{n_2} T_2}$$

$$\frac{0.80 \text{ atm}}{298 \text{ K}} = \frac{0.30 \text{ atm}}{T_2}$$

do NOT use °C in Gas Law equations
 $T_2 \neq 9.4^{\circ}\text{C}$

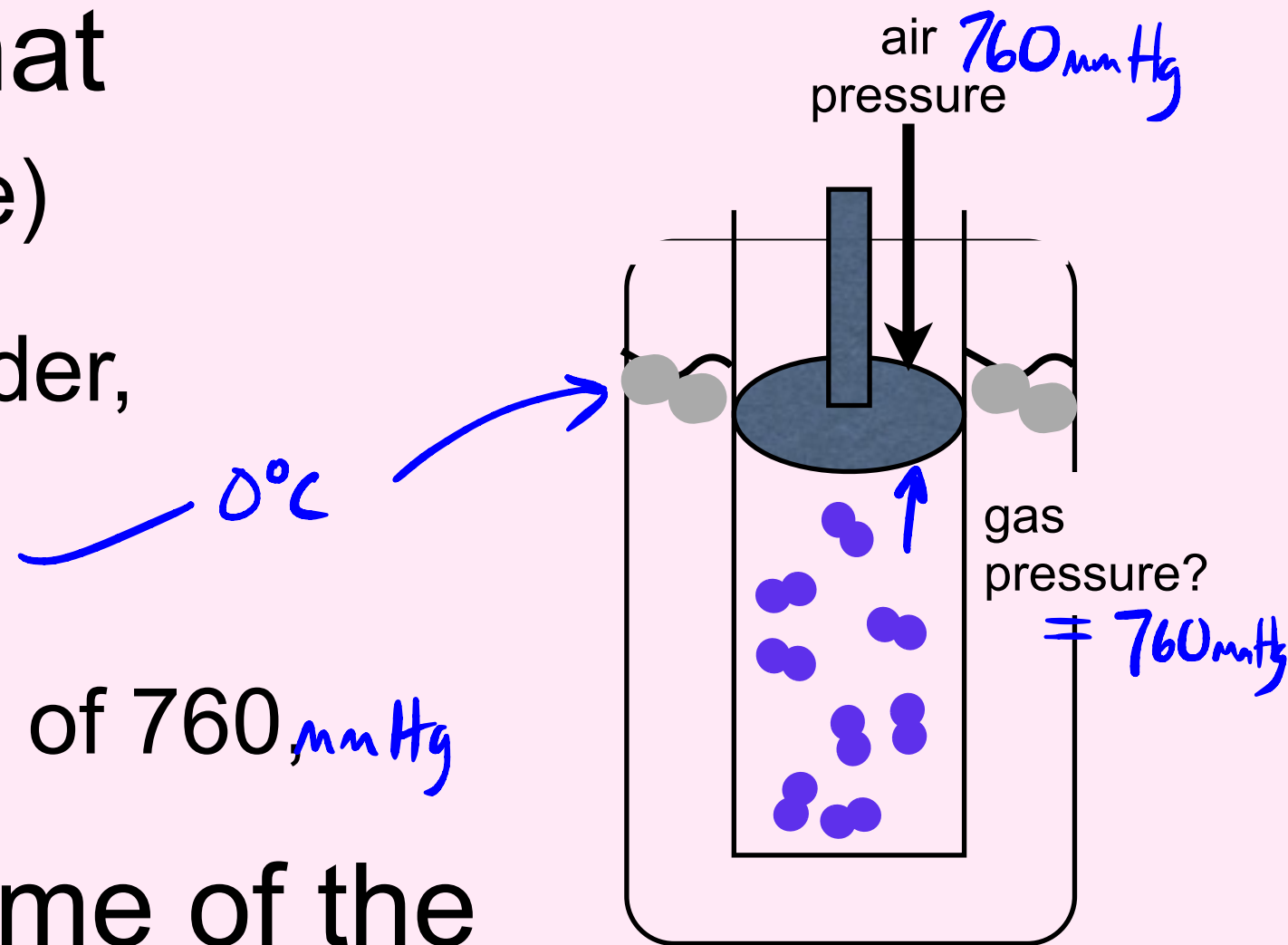
$$T_2 = 112 \text{ K}$$
$$\frac{-273}{T_2 = -161^{\circ}\text{C}}$$

Developing the Ideal Gas Law

Just a Manifestation of
the Combined Gas Law

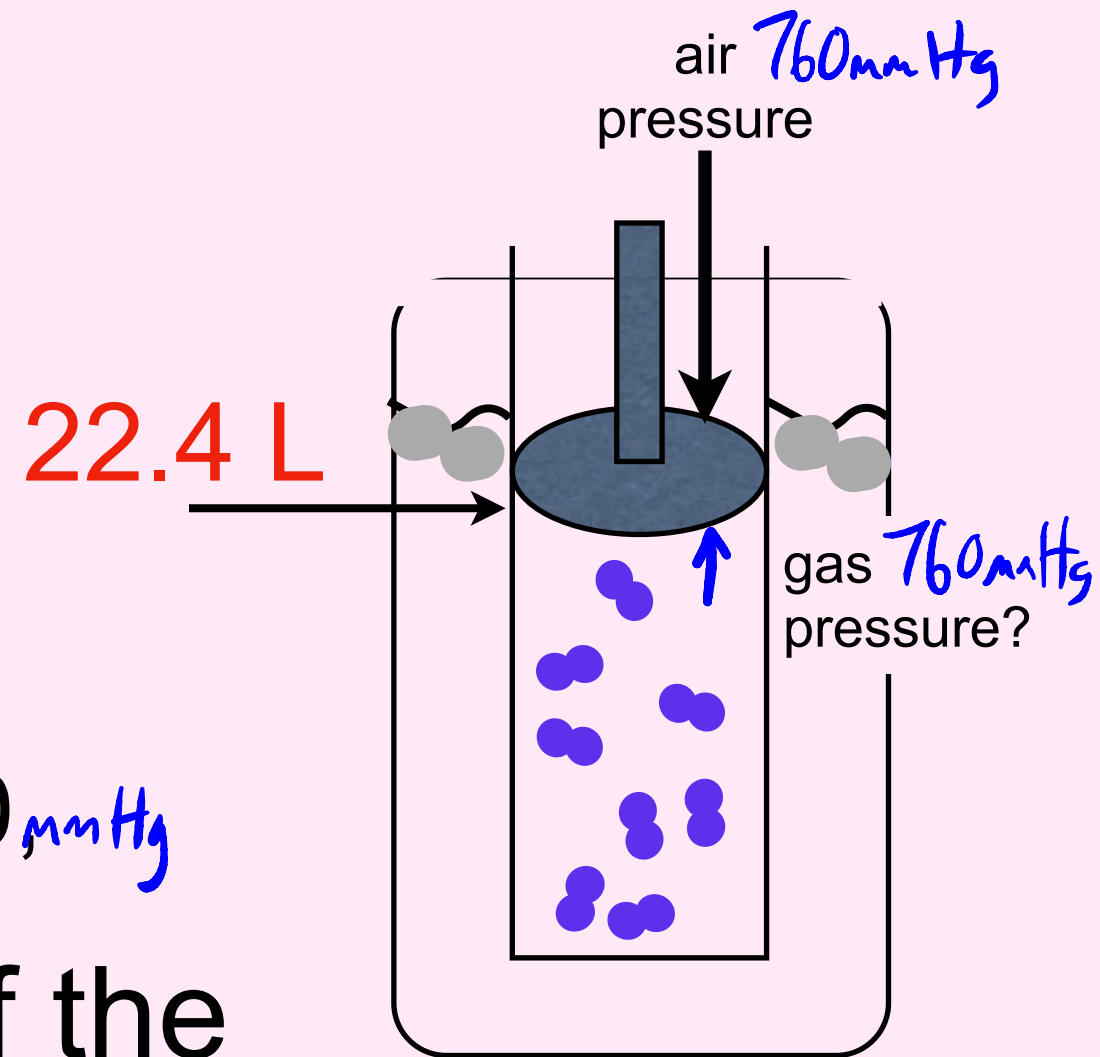
Measurements of O₂ gas at particular conditions...

- It just so happens that
 - ✓ 32 g of oxygen, (1 mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water, 0°C
 - ✓ barometric air pressure of 760 mmHg
- The measured volume of the gas will be ???



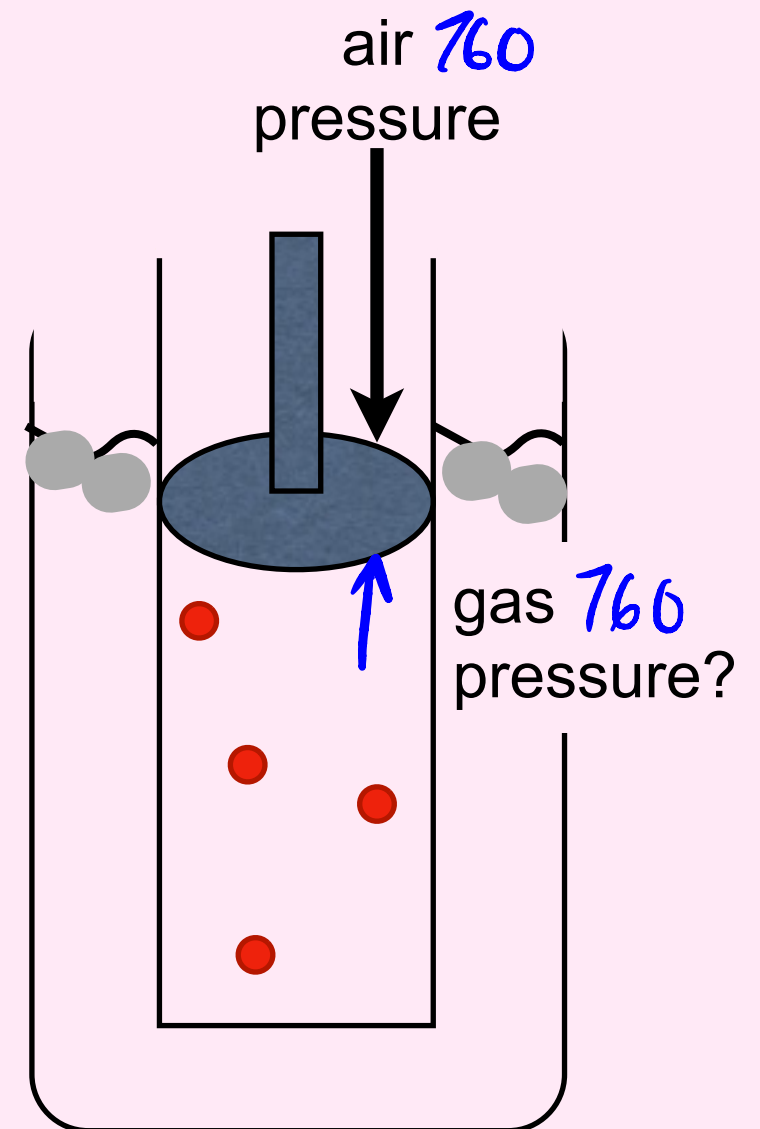
Measurements of O₂ gas at particular conditions...

- It just so happens that
 - ✓ 32 g of oxygen, (1 mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water,
 - ✓ barometric air pressure of 760_{mmHg}
- The measured volume of the gas will = 22.4 L



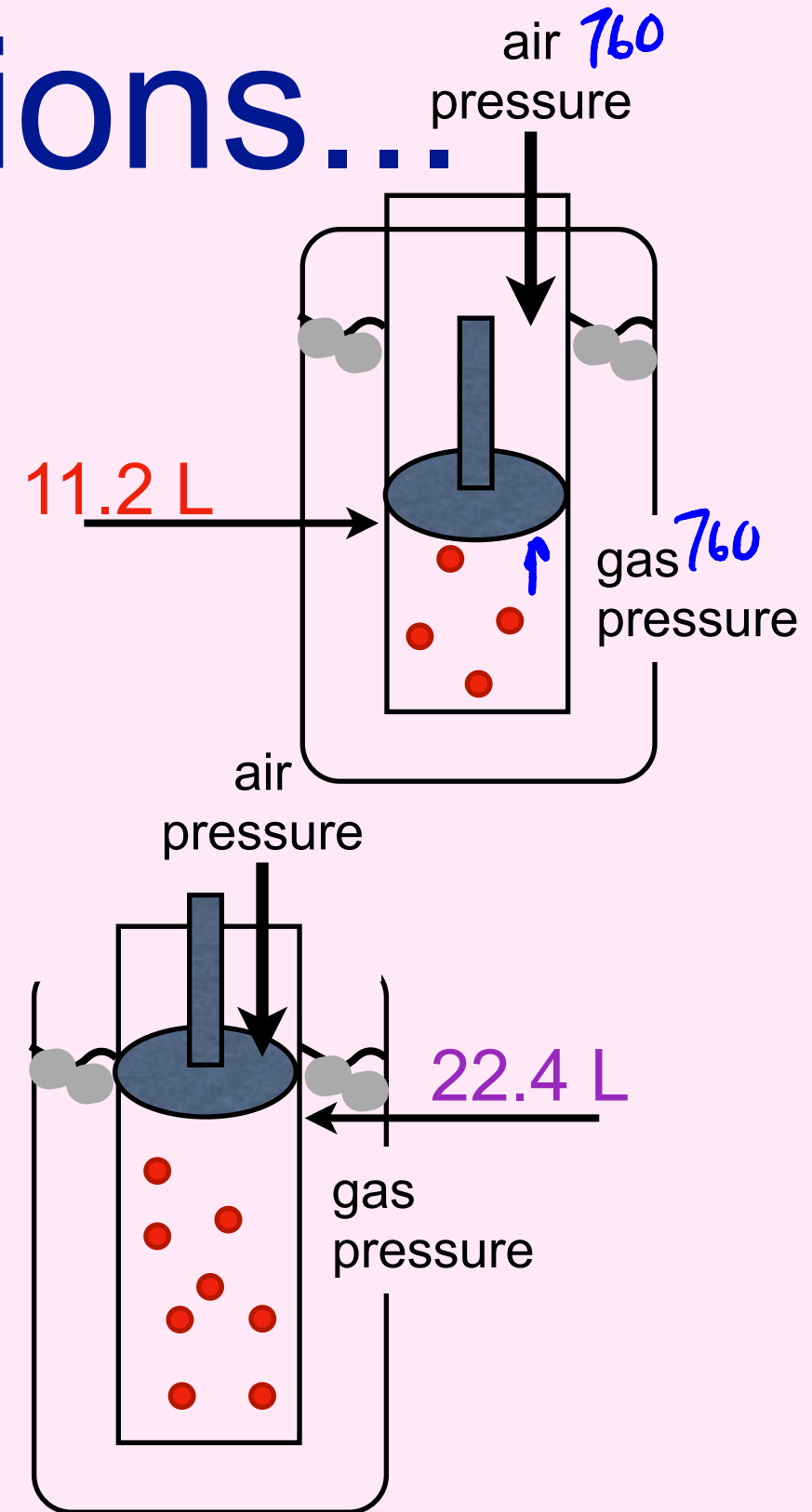
Measurements of He gas at particular conditions...

- It just so happens that
 - ✓ 2 g of helium, ($\frac{1}{2}$ mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water,
 - ✓ barometric air pressure of 760,
- The measured volume of the gas will = ???



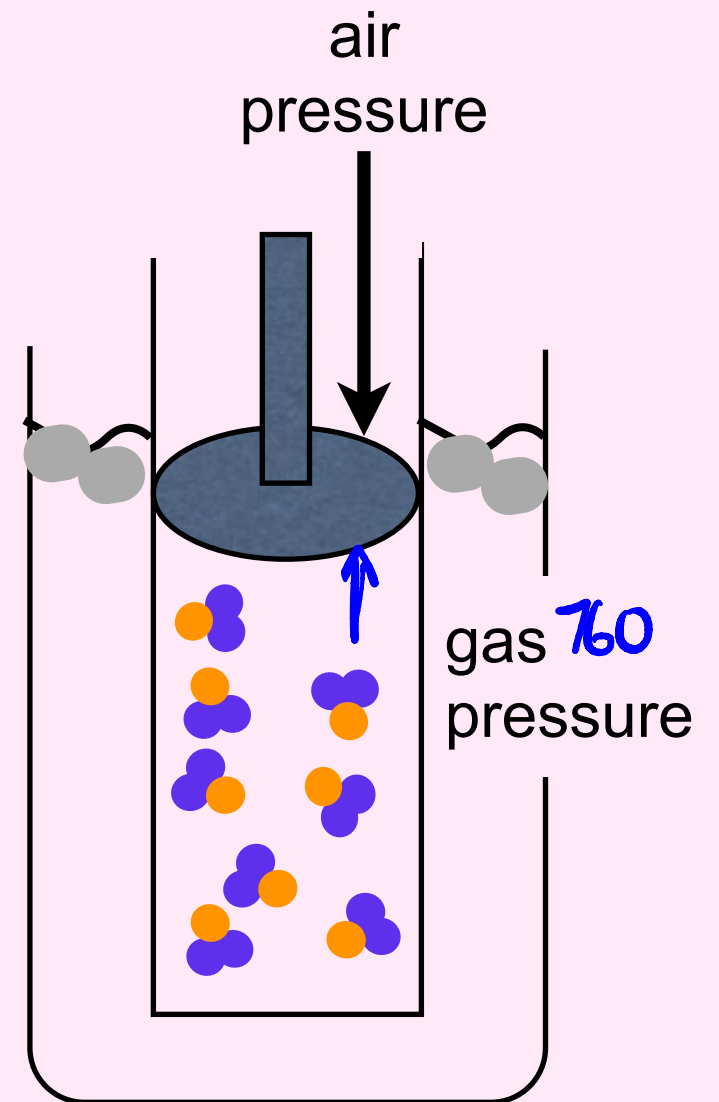
Measurements of He gas at particular conditions...

- It just so happens that
 - ✓ 2 g of helium, ($\frac{1}{2}$ mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water,
 - ✓ barometric air pressure of 760 mmHg
- The measured volume of the gas will = 11.2 L
- When increased to 4 g, the volume of the gas = 22.4 L



Measurements of CO₂ gas at particular conditions...

- It just so happens that
 - ✓ 44 g of CO₂, (1 mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water,
 - ✓ barometric air pressure of 760 *mmHg*
- The measured volume of the gas will = ???



Measurements of CO₂ gas at particular conditions...

- It just so happens that
 - ✓ 44 g of CO₂, (1 mole)
 - ✓ sealed in a piston cylinder,
 - ✓ plunged into ice water,
 - ✓ barometric air pressure of 760_{mmHg}

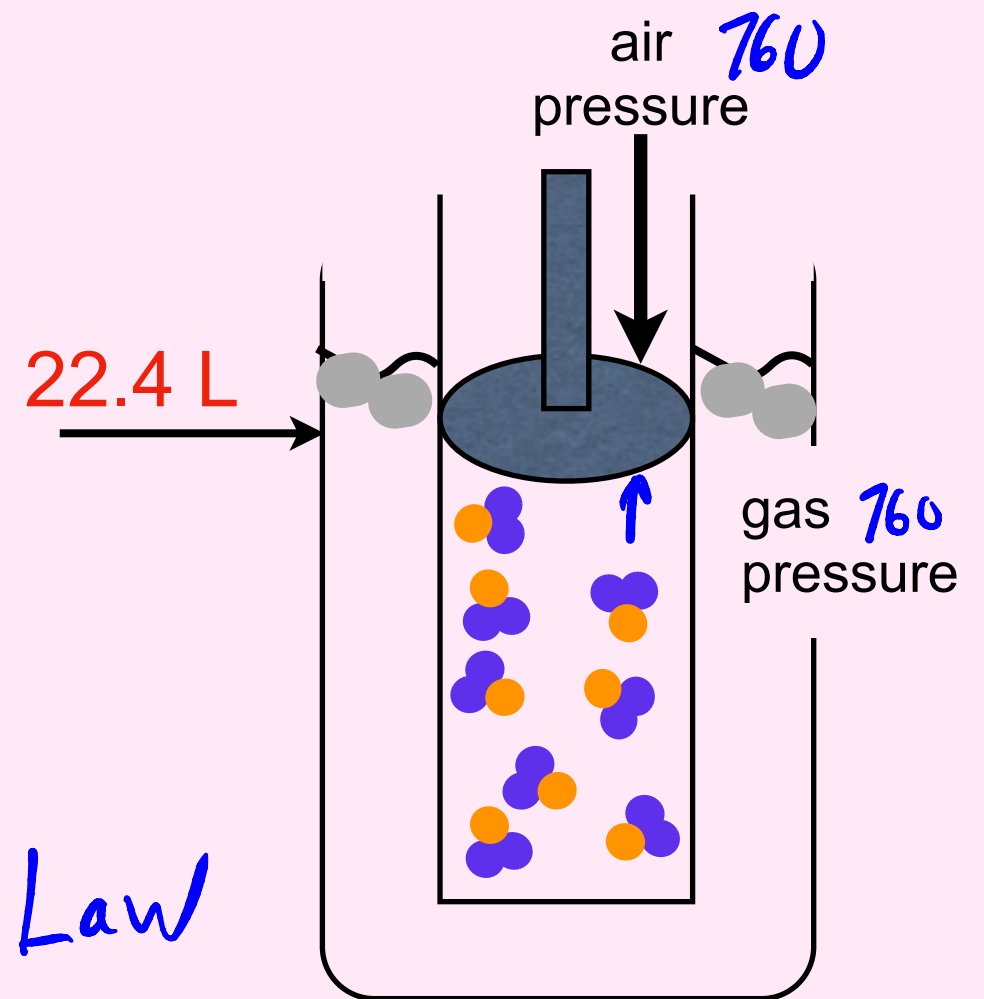
- The measured volume of the gas will = 22.4 L, yet again!

- Something is going on here... Avogadro's Law

- There must be some relationship between the proportions of P, V, n, and T for any gas

$$\frac{PV}{nT}$$

Let's plug in some of these measured values and calculate.



The Ideal Gas Constant, R

✓ 44 g of CO₂, (1 mole)

✓ plunged into ice water, 0°C = 273 K

✓ barometric air pressure of 760 mmHg

✓ 22.4 L

$$\frac{PV}{nT}$$

- Plug these values into one side of the Combined Gas Law, and solve

$$\frac{760 \text{ mmHg} \times 22.4 \text{ L}}{1 \text{ mol} \times 273 \text{ K}} = 62.4 \text{ mmHg} \cdot \text{L} \cdot \text{mol}^{-1} \text{K}^{-1}$$

or $\frac{62.4 \text{ mmHg} \cdot \text{L}}{\text{mol} \cdot \text{K}}$

- Since the same proportional values will exist for any gas, this number is a constant.
- The Ideal Gas Constant, R

Different Values for R?

- The units on the gas constant R are very important.
- If we plug the values into the gas law measuring in different units, R will be different.

$$\frac{PV}{nT} = R$$

$$\frac{760 \text{ mmHg} \times 22.4 \text{ L}}{1 \text{ mol} \times 273 \text{ K}} = 62.36 \text{ mmHg} \cdot \text{L} \cdot \text{mol}^{-1} \text{K}^{-1}$$

Still the Gas constant, R, different units

$$\frac{1 \text{ atm} \times 22.4 \text{ L}}{1 \text{ mol} \times 273 \text{ K}} = 0.08206 \text{ atm} \cdot \text{L} \cdot \text{mol}^{-1} \text{K}^{-1}$$

Voila, The Ideal Gas Law

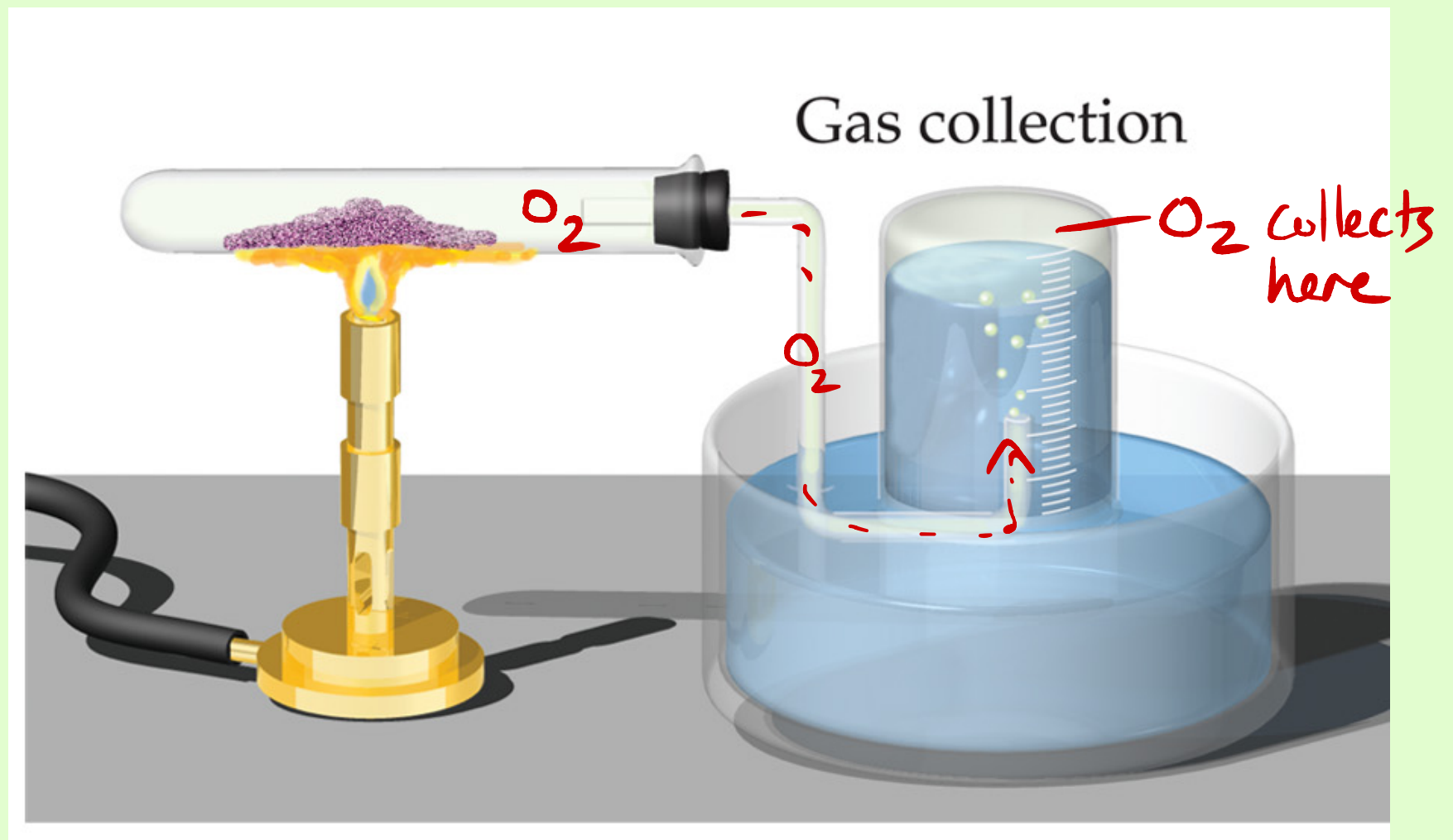
$$\frac{PV}{nT} = R$$

$$PV = nRT$$

- This will be very useful to us as we work stoichiometry problems for reactions that involve gases.

Collecting gas from a Rxn

- Consider the decomposition of potassium chlorate into potassium chloride and oxygen gas.
- Write a balanced chemical equation for this reaction.





KClO_3 122.55 g/mol

- Suppose you decomposed 1.72 g of potassium chlorate, what volume of oxygen could be produced if the oxygen were collected at 25°C at 740 mmHg pressure?

$$PV = nRT$$

Answer 
on next slide

$$R = 62.4 \text{ L}\cdot\text{mmHg/mol}\cdot\text{K} \quad \text{or} \quad R = 0.0821 \text{ L}\cdot\text{atm/mol}\cdot\text{K}$$



KClO₃ 122.55 g/mol

- Suppose you decomposed 1.71 g of potassium chlorate, what volume of oxygen could be produced if the oxygen were collected at 25°C at 740 mmHg pressure?

$$1.71 \text{ g KClO}_3 \times \frac{1 \text{ mol KClO}_3}{122.5 \text{ g KClO}_3} \times \frac{3 \text{ mol O}_2}{2 \text{ mol KClO}_3} = 0.0209 \text{ mol O}_2$$

$$PV = nRT$$

$$V = \frac{nRT}{P}$$

$$V = \frac{0.0209 \text{ mol} \times 62.4 \text{ L mmHg} \times 298 \text{ K}}{740 \text{ mmHg}}$$

$$V = 0.526 \text{ L of O}_2 \quad (526 \text{ ml})$$